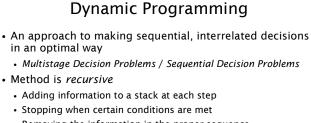
Optimization Theory MT 610	
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Dynamic Programming	
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- Removing the information in the proper sequence
- Optimize part of the problem, then use that solution to optimize a slightly larger problem. Keep increasing the size of the problem until it encompasses the original problem. (Ex: *Dykstra's shortest path algorithm*)

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## Characteristics

- Stages
- States at each Stage
- Decision at each Stage
  - · Decision updates the State for the next Stage
  - Optimum decision for remaining Stages is *independent* of decisions at previous Stages
- *Recursive relationship* between value of decision at current Stage and the value of optimum decisions at earlier stages
- Often stages are sequenced in time, hence the name dynamic programming. Optimizing the answer to the "What next?" question

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## Recursion

- Shortest path example
  - Shortest path to node i = minimum { Shortest path to solved nodes j + Distance from j to l}
  - Shortest path on both sides
- New optimum derived from old optimum along with some local value
- Recursive relation can be addition, multiplication or even something more abstract and general

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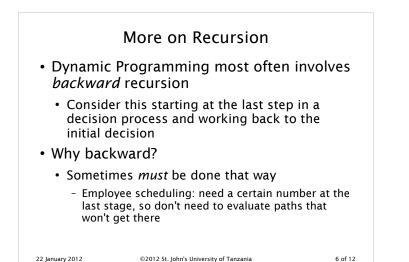
## Formulating the Solution

- What are the *stages* in the solution?
- How is the state defined at a stage?
- What kind of *decision* must you make at a stage?
- How does the decision *update* the state for the next stage?
- What is the *recursive* value relationship between the optimum decision at a stage and a previous optimum decision?

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## Example 1 Equipment Replacement (Chinneck, 2010, Ch15, p3) Objective function cost of ownership = acquisition + maintenance - scrap value Stages = time frames, overall & incremental

- Decision = buy or keep at each stage
- End stage = must have a functioning piece of equipment at the end of the overall time frame

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- Specific case: Bicycle over five years
- Recursion is additive

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